

Parabola Notes

$$y = x^2$$

$$y = ax^2 + bx + c$$

Standard Form

$$y - k = \pm a(x - h)^2 \quad \text{or} \quad x - h = \pm a(y - k)^2$$

+ opens up vertex (h,k)

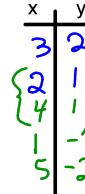
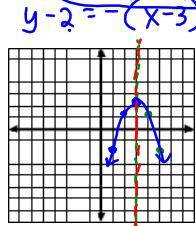
- opens down

+ opens right vertex (h,k)

- opens left

Accurately graph the parabola. State the vertex, domain, range, axis of symmetry, "a" value, and direction.

1. $y = -(x - 3)^2 + 2$ 5 points



a) the vertex (3, 2)

b) the axis of symmetry

c) Domain $\{x \in \mathbb{R}\}$

x = 3

d) Range $y \leq 2$

y ≤ 2

e) "a" value

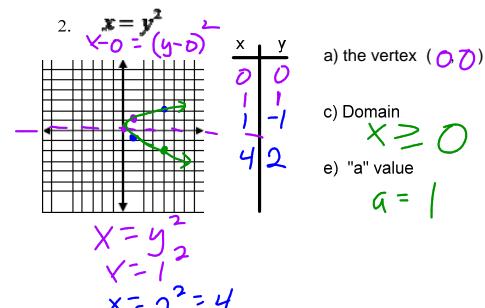
a = 1

f) direction of opening

opens down

$$\begin{aligned} y &= -(2-3)^2 + 2 \\ &= -(-1)^2 + 2 \\ &= -1 + 2 = 1 \end{aligned}$$

$$y = -(1-3)^2 + 2 = -2$$



a) the vertex (0, 0)

b) the axis of symmetry

c) Domain $x \geq 0$

y = 0

d) Range $\{y \in \mathbb{R}\}$

TR

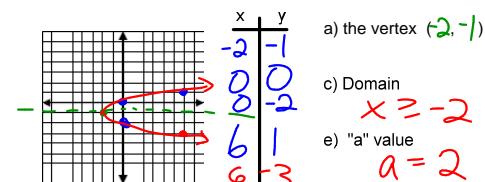
e) "a" value

f) direction of opening

a = 1

right

3. $x + 2 = 2(y + 1)^2$



a) the vertex (-2, -1)

b) the axis of symmetry

c) Domain $x \geq -2$

y = -1

d) Range $\{x \in \mathbb{R}\}$

TR

e) "a" value

f) direction of opening

a = 2

right

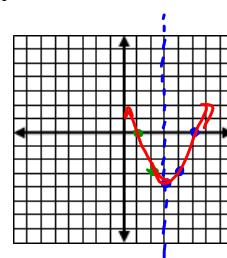
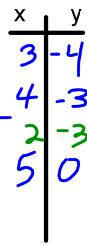
$$x = 2(y + 1)^2 - 2$$

$$x = 2(0 + 1)^2 - 2 = 0$$

$$x = 2(1 + 1)^2 - 2 = 6$$

Not everything is in standard form, so you must complete the square to put it into standard form.

$$\begin{aligned}
 4. \quad & x^2 - 6x - y + 5 = 0 \\
 & +y - 5 +y - 5 \\
 & x^2 - 6x + 9 = y - 5 + 9 \\
 & (x-3)^2 = y + 4 \\
 & y + 4 = (x-3)^2 \\
 & y = (x-3)^2 - 4 \\
 & y = (4-3)^2 - 4 = -3 \\
 & y = (5-3)^2 - 4 = 0
 \end{aligned}$$



a) the vertex $(3, -4)$

b) the axis of symmetry

c) Domain \mathbb{R}

d) Range $y \geq -4$

e) "a" value

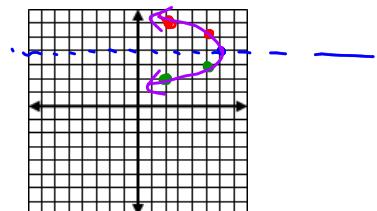
$$a = 1$$

f) direction of opening

up

Complete the Square

$$\begin{aligned}
 5. \quad & y^2 - 8y + x + 10 = 0 \\
 & -x - 10 -x - 10 \\
 & y^2 - 8y + 16 = -x - 10 + 16 \\
 & (y-4)^2 = -x + 6 \\
 & -x + 6 = (y-4)^2 \\
 & \boxed{x-6 = -(y-4)^2} \\
 \text{Need } & \text{standard form} \\
 X & X = -(y-4)^2 + 6 \\
 \text{not } & X = -(5-4)^2 + 6 = 5 \\
 -X & X = -(6-4)^2 + 6 = 2
 \end{aligned}$$



a) the vertex $(6, 4)$

b) the axis of symmetry

c) Domain $x \leq 6$

d) Range $y \in \mathbb{R}$

e) "a" value

$$a = 1$$

f) direction of opening

left

6. $2x^2 - 8x - y + 10 = 0$

$$+y - 10 + y - 10$$

$$\begin{aligned} 2x^2 - 8x &= y - 10 \\ 2(x^2 - 4x + 4) &= y - 10 + 2(4) \end{aligned}$$

$$2(x-2)^2 = y - 2$$

$$\boxed{y - 2 = 2(x-2)^2}$$

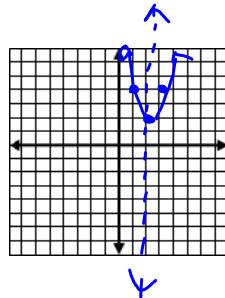
standard form

$$y = 2(x-2)^2 + 2$$

$$y = 2(3-2)^2 + 2$$

$$y = 2(4-2)^2 + 2 = 10$$

x	y
2	2
3	4
4	10
2	4
0	10



a) the vertex $(2, 2)$

b) the axis of symmetry

$$x = 2$$

c) Domain \mathbb{R}

d) Range

$$y \geq 2$$

e) "a" value

$$a = 2$$

f) direction of opening

up